

# A Deep Neural Networks Assisted Channel Estimation and Decoding for MIMO

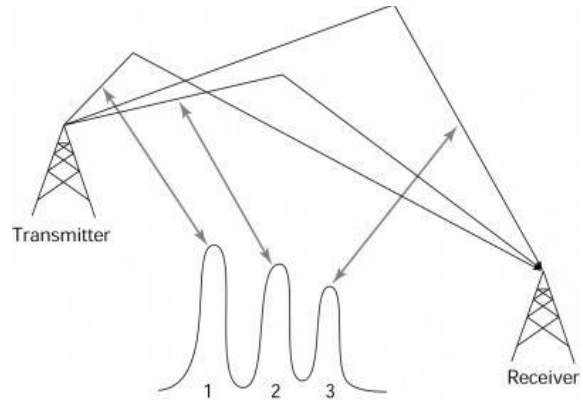
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**Abstract**— Present day communication systems are facing some critical issues which are increased number of users, the amount of bandwidth availability to be used by the users and the need for ever increasing data rates. The major concern regarding all the problems is the high capacity expectation from wireless channels. However, wireless channels are often random in nature with frequency selective nature at the base. The limitation in the bandwidth support by any channel makes the data rate support to be limited. In this paper, a deep neural network assisted massive MIMO system has been designed and has been employed to commonly existing diverse channel conditions. To increase the spectral efficiency and simultaneously reduce the BER of the system, the Maximum Ratio Combining (MRC) approach has been used along with MMSE and ZFE equalization techniques. The proposed system has been simulated on Matlab. The performance of the system has been evaluated in terms of the Bit Error Rate and Spectral Efficiency of the system.

**Keywords**—Multiple Input Multiple Output (MIMO), Deep Neural Networks, Maximum Ratio Combining (MRC), Zero Forcing Equalizer, Minimum Mean Square Error (MSE), Bit Error Rate (BER), Spectral Efficiency.

## I. INTRODUCTION

MIMO systems are the need of the hour due to the capability to increase channel capacity even at limited bandwidth systems. Practical channels seldom follow the ideal characteristics of gain and phase response. However, the degradation of the BER performance of MIMO systems is a serious concern to achieve satisfactory QoS. Off late machine learning and artificial intelligence based techniques are being explored for MIMO equalizer design due to the fact that such systems are capable of pattern recognition for large datasets in limited time.



**Fig.1 Multipath Propagation**

Multi-path propagation results in the non-ideal characteristics of channel response which happen to be a constant gain response with respect to frequency and an negative linear phase response with respect to frequency. The conditions can be mathematically represented as:

$$H(\omega) = K \forall \omega \quad (1)$$

$$P(\omega) = -l(\omega) \forall \omega \quad (2)$$

Here,

$H(\omega)$  represents the magnitude response of the channel.

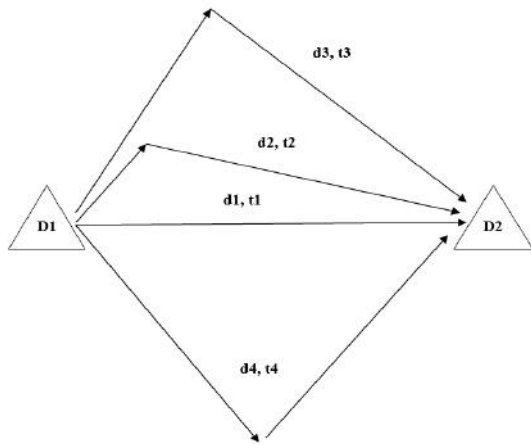
$P(\omega)$  represents the phase response of the channel.

$\omega$  represents the angular frequency given by:

$$\omega = 2\pi f \quad (3)$$

$K$  is a constant

$-l(\omega)$  represents a linear function



**Fig.2 Effect of Multipath Propagation**

Multipath propagation results in a non-ideal impulse response of the system. The aforesaid factors makes it mandatory to design equalizers which can reverse the negative effects of the non-ideal channel

Another problem arising out of multi-path propagation mechanisms is the distributed impulse response of system given by:

$$h(\omega) = h_1g_1 + \dots \dots \dots h_n g_n \quad (4)$$

or

$$h(\omega) = \sum_{i=1}^n h_i g_i \quad (5)$$

Here,

$h(\omega)$  is the composite impulse response

$h_i$  is the individual impulse response of a particular path

$g_i$  denotes the individual path gain of a path.

Thus a composite signal comprising of multiple copies of the data results in the overlap of signals causing interference often leading to a Poisson based distribution. The probability distribution function of such a distribution (which governs the receiver power) is given by:

$$P(X, n) = \text{Prob}(X = n) = \frac{Z^n e^{-Z}}{n!} \quad (6)$$

Here,

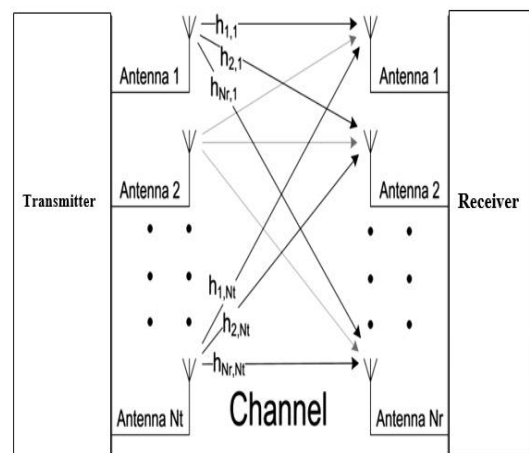
X denotes the random variable

n denotes the occurrence number

e denotes the Euler's constant.

With respect to the present scenario, Z denotes the received power and 'n' denotes the number of multi path components in the communication media.

As the available radio spectrum is limited, higher data rates can be achieved only by designing more efficient signalling techniques. Recent research in information theory has shown that large gains in capacity of communication over wireless channels are feasible in multiple input multiple output (MIMO) systems as well as significantly enhances the system performance compared to conventional systems in fading multipath channel environment. The MIMO channel is constructed with multiple element array antennas at both ends of the wireless link. All these MIMO techniques are based on proper handling of (Alamouti scheme and maximum ratio combining method) signals transmitted and received by an array of antennas. Simulation results show very high performance in terms of bit error rate, even for low signal-to-noise ratio Multiple Input Multiple Output (MIMO) systems are once such avenue [3]. MIMO systems increase the channel capacity manifold compared to Single Input Single Output (SISO) systems thereby enabling higher data rate transmission for the same bandwidth. MIMO technology has attracted attention in wireless communications, because it offers significant increases in data throughput and link range without additional bandwidth or transmit power. It is achieved by higher spectral efficiency (more bits per second per hertz of bandwidth) and link reliability or diversity (reduced fading). Because of these properties, MIMO is an important part of modern wireless communication standards such as IEEE 802.11n(Wifi), 4G, 3GPP Long Term Evolution, WiMAX and HSPA. The schematic for a typical MIMO system is depicted in figure 3.



**Fig.3. Conceptual model of a MIMO system**

The MIMO based system has multiple transmitter and multiple receivers which create parallel data paths

for transmission and reception which in turn allows enhanced data rates for the same limited bandwidth [4]. To implement this MIMO based transmission scheme practically, Space Time Block Coding (STBC) is often employed in which the data stream is arranged as a matrix with the number of columns equating to the number of MIMO transmitters and the number of rows equating to the number of time slots of transmission. The symbols of STBC transmission can be estimated as:

$$\mathbf{H}^+ = (\mathbf{H}^H \mathbf{H})^{-1} \mathbf{H}^H \quad (7)$$

Here,

$\mathbf{H}^+$  represents the Moore-Penrose pseudo inverse since the channel matrix,

$\mathbf{H}$  is the channel matrix and it may not always be square for the STBC matrix. Typically, the channel capacity is enhanced as per the following relation:

$$\mathbf{C} = f\{kBlpg_2 \left[ 1 + \frac{h_{ij}^2 S}{N} \right]\} \quad (8)$$

Here,

$\mathbf{C}$  is the channel capacity

$\mathbf{B}$  is the channel bandwidth

$\mathbf{S}$  is the signal power

$\mathbf{N}$  is the noise power

$k$  is a constant depending on system parameters

$f$  is a function depending on system parameters

$h$  is the MIMO channel matrix

$i$  is the number of transmitters

$j$  is the number of receivers

Here,

$x_1, x_2 \dots x_n$  are the different sub-carriers for OFDM transmission

$n$  is the total number of carriers

$T$  is the period of the carriers

The system comprising of MIMO-OFDM suffers from frequency selective nature of channels and thereby encounters degraded BER performance in general [6]-[7].

## II. MACHINE LEARNING ASSISTED MIMO SYSTEM DESIGN

As mentioned earlier, the data being transmitted and received is staggeringly large which makes it extremely challenging to accurately estimate the channel characteristics in time critical applications. Hence, neural networks are being used off late to accurately estimate channel characteristics. A typical

mathematical equivalent of a neuron is depicted in figure 4. It is a neuron with multiple inputs.

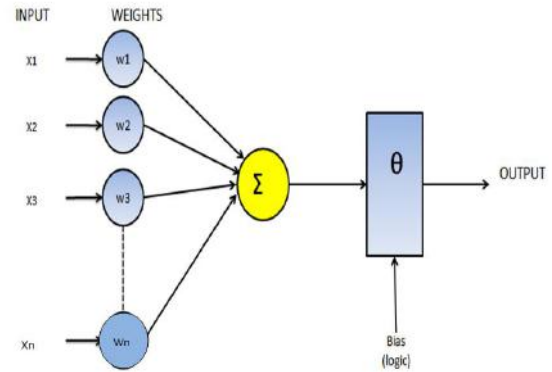


Fig.4 Mathematical Model of Neuron

In case the neurons are connected to each other to render a network, the neural network is depicted in figure 5.

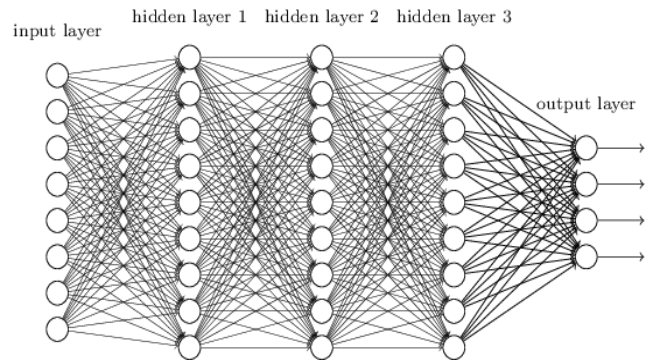


Fig.5 A typical Neural Network

The neural network is employed to estimate the channel characteristics in the following manner:

**Step 1.** Generate dummy data (binary stream) for training.

**Step 2.** Pass the data through the channel.

**Step 3.** Provide the equalizer (Neural Network Based) with the data being sent originally and the stream after passing through channel.

**Step 4.** Design a training Rule.

**Step 5.** Use the channel state information to perform equalization.

**Step 6.** Compute the BER of the system.

A typical training rule can be given by:

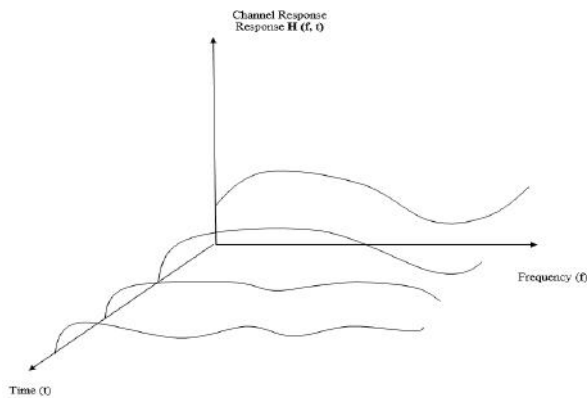
$$\mathbf{w}_{k+1} = \mathbf{w}_k - [\mathbf{J}_k \mathbf{J}_k^T + \mu \mathbf{I}]^{-1} \mathbf{J}_k^T \mathbf{e}_k \quad (9)$$

Here,  
 W are the weights  
 K is the iteration number  
 e is the error  
 J is the Jacobian

The BER-SNR relation is plotted for simulation as:

$$\left(\sum_{i=1}^n \forall \text{all bits 'n' as a function of SNR}\right) \quad \text{Bit}_{RX} \neq \text{Bit}_{TX} \quad (10)$$

Typically, wireless channels depicts frequency selective nature i.e. they behave differently for different frequencies. Moreover, the frequency selectivity is not fixed by also exhibits temporal variation [8].



**Fig. 6. Frequency Response of typical wireless channels**

The composite impulse of the wireless channels corresponding to multi-path propagation effects can be given by:

$$h(t) = \sum_{i=1}^n h_n \quad (11)$$

Here,  
 h(t) is the composite impulse response of the channel.  
 h(n) corresponds to each of the responses to single tone frequencies.

To convert the impulse response of the channel into the time domain, we compute the Fourier Transform given by:

$$H(f) = \int_{-\infty}^{\infty} h(t)e^{-j\omega t} dt \quad (12)$$

Here,  
 H(f) is the channel response in frequency domain  
 $\omega$  is the angular frequency  
 The sampled version of the channel response is given by:

$$H(f, nT_s) = \sum_{i=1}^n H(f, t - nT_s) \quad (13)$$

Here,  
 Ts is the sampling time for channel sounding  
 n is the number of samples  
 f is the frequency metric

For OFDM transmission, often to reduce the effects of frequency selectivity of channels, the cyclic prefix (CP) is inserted and is given by:

$$S_{CP} = S_n - S_{n-k} \quad (14)$$

Here,  
 $S_{CP}$  is the samples in the cyclic prefix  
 S is the original signal  
 n are the total number of samples  
 (n-k) are the samples which are appended as the cyclic prefix

Noise effects in case of wireless channels are inevitable and it becomes even more prominent with different paths of the MIMO system seeing a slightly different channel condition [9]-[10]. Thus it becomes necessary to mitigate the effects of such a frequency selective channel. It can be done by the design of an equalizer which tries to revert the effects of the channel. The design of the equalizer requires the information regarding the channel response h(f). Since any practical system can sense the channel in the discrete time domain, therefore the channel impulse response can be re-considered as h(n) [11]. Let the channel in the frequency domain be H(z). Then the output of the channel is:

$$y(n) = x(n) * h(n) \quad (15)$$

$$Y(z) = X(z) \cdot H(z) \quad (16)$$

Where, \* stands for convolution  
 x(n) is the input to the channel  
 y(n) is the output of the channel  
 The aim at design of an equalizer is the design of a system with a transfer function

$$E(z) = \frac{1}{H(z)} \quad (17)$$

The equalizer is placed just before the receiver and its performance depends greatly upon the accuracy with which the channel is estimated in the first place [12]. While there are different equalization techniques which can be employed, equalization used in the proposed system is the deep learning assisted zero forcing

equalization which owing to its relative simplicity of implementation can be incorporated with massive MIMO systems [16]. The mathematical formulation for the block linear equalizer (BLE) with zero forcing (ZF) approach is mathematically is given by:

$$\hat{\mathbf{d}}_{c,ZF-BLE} = (\mathbf{A}^H \mathbf{R}_n^{-1} \mathbf{A})^{-1} \mathbf{A}^H \mathbf{R}_n^{-1} \mathbf{e} \quad (18)$$

Or,

$$\hat{\mathbf{d}}_{c,ZF-BLE} = \mathbf{d} + (\mathbf{A}^H \mathbf{R}_n^{-1} \mathbf{A})^{-1} \mathbf{A}^H \mathbf{R}_n^{-1} \mathbf{n} \quad (19)$$

Here,

$\hat{\mathbf{d}}_{c,ZF-BLE}$  represents the zero forcing term

$\mathbf{d}$  are the desired symbols

$(\mathbf{A}^H \mathbf{R}_n^{-1} \mathbf{A})^{-1} \mathbf{A}^H \mathbf{R}_n^{-1} \mathbf{n}$  is the residual noise term

$\mathbf{H}$  is the MIMO channel response

$\mathbf{R}_n$  is the Choleski decomposition of a conventional matched filter at the receiver

$\mathbf{A}^H \mathbf{R}_n^{-1}$  is the response of a typical whitening matched filter.

The SNR per symbol at the output of the ZF-BLE is given by:

$$\gamma_{ZF-BLE}(\mathbf{k}, \mathbf{n}) = \frac{E\{|\mathbf{d}_n^k|^2\}}{(\mathbf{A}^H \mathbf{R}_n^{-1} \mathbf{A})_{i,j}^{-1}} \quad (20)$$

Here,

$E$  is the expectation of average value of the random variable

$\mathbf{n}$  is the symbol number

$\mathbf{k}$  is the number of samples

Considering correctness at the output of the ZFE, the output is given by [17]:

$$\gamma_{ZF-BLE}(\mathbf{k}, \mathbf{n}) = E\{|\mathbf{d}_n^k|^2\} |\Sigma|_{i,j}^2 \quad (21)$$

The Minimum Mean Square Error (MMSE) algorithm tries to minimize the mean square error as the objective function (G)

Here, the errors in channel estimation can be minimized by employing the following relation:

$$\mathbf{G} = \text{minimize} \left( \frac{1}{n} \sum_{i=1}^n e_i^2 \right) \quad (22)$$

Here,

$\mathbf{G}$  denotes the objective function

$e$  denotes current error sample value

$n$  denotes the number of error samples

The zero forcing equalizer tries to force the mean square error (mse) of the channel estimation to zero.

Mathematically, equalization is performed if,

$$\mathbf{x}(\mathbf{k}) = [\mathbf{0}_M \quad \mathbf{I}_M] \begin{bmatrix} \mathbf{u}(\mathbf{k}-1) \\ \mathbf{u}(\mathbf{k}) \end{bmatrix} + E \frac{W_M}{\sqrt{M}} \mathbf{Z}_r r(\mathbf{k}) \quad (23)$$

Here,

$M \times M$  is the matrix size

$\mathbf{u}$  is the received signal

$\mathbf{x}$  is the recovered or equalized signal

$\mathbf{W}$  are the weights of the equalizer

$E$  is the expectation or average value

### III. SIMULATION RESULTS

The system has been designed on Matlab 2020a. The neural network design and the subsequent BER evaluation is presented.



Fig. 7. Designed Deep Neural Network

The performance of the proposed system is evaluated in terms of the bit error rate (BER). This is also indicative of the actual channel capacity of the channel in terms of the error free data transmission.

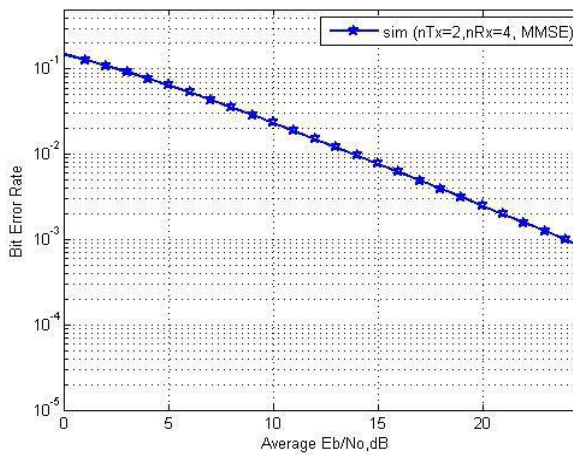


Fig. 8. BER Analysis for 2X4 MIMO with MMSE

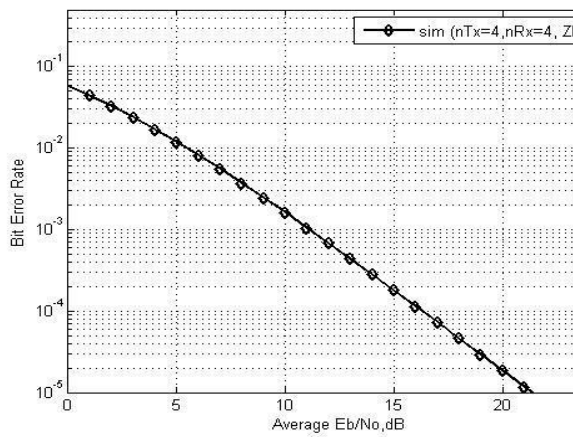


Fig.9. BER Analysis for 2X4 MIMO with ZFE

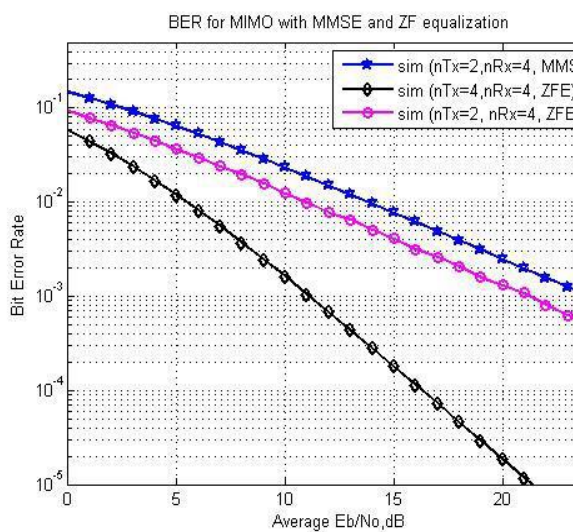


Fig. 10. BER Analysis for 2X4 and 4X4 MIMO with MMSE and ZFE

The BER Analysis for the system is tabulated in Table I

**TABLE I**  
**COMPARATIVE BER ANALYSIS FOR THE**  
**DICERSITY SCHEME**

System	Least BER	SNR Needed
DNN-MMSE	$10^{-3}$	25dB
DNN-ZFE	$10^{-5}$	20dB
Tx=2, Rx=2	In between $10^{-3}$ and $10^{-4}$	20dB
Tx=4, Rx=4	$10^{-5}$	20dB
Guo et al., 2023	$10^{-3}$	30dB
Liu et al., 2022	$10^{-2}$	20dB

From the results of Table I, it can be clearly observed that the proposed work outperforms contemporary work in the domain by achieving lower BER at lesser SNR requirement compared to recent work (Gua et al., and Liu et al.) This would mean that the proposed system attains higher accuracy of channel estimation rendering better Quality of Service (QoS) compared to existing work in the domain.

#### IV. CONCLUSION

It can be concluded from the previous discussions that MIMO systems can be considered to be key enablers in high data rate wireless communications. In the proposed approach, a comparative analysis of OFDM transmission and a combination of OFDM and MIMO has been done. Due to multi path propagation and fading effects, it becomes necessary to employ channel estimation and MIMO decoding in conjugation with equalization. Two deep learning assisted techniques employing MMSE and ZFE techniques are proposed. It can also be concluded that ZFE performs better than the MMSE approach for equalization for MIMO systems. Moreover a comparative analysis with existing work clearly indicates that the proposed work outperforms existing work in terms of error rate, SNR requirement thereby enhancing QoS for massive MIMO systems

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